

Simultaneous Measurement of Three-Dimensional Joint Kinematics and Ligament Strains With Optical Methods

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The objective of this study was to assess the precision and accuracy of a nonproprietary, optical three-dimensional (3D) motion analysis system for the simultaneous measurement of soft tissue strains and joint kinematics. The system consisted of two high-resolution digital cameras and software for calculating the 3D coordinates of contrast markers. System precision was assessed by examining the variation in the coordinates of static markers over time. Three-dimensional strain measurement accuracy was assessed by moving contrast markers fixed distances in the field of view and calculating the error in predicted strain. Three-dimensional accuracy for kinematic measurements was assessed by simulating the measurements that are required for recording knee kinematics. The field of view (190 mm) was chosen to allow simultaneous recording of markers for soft tissue strain measurement and knee joint kinematics. Average system precision was between ± 0.004 mm and ± 0.035 mm, depending on marker size and camera angle. Absolute error in strain measurement varied from a minimum of $\pm 0.025\%$ to a maximum of $\pm 0.142\%$, depending on the angle between cameras and the direction of strain with respect to the camera axes. Kinematic accuracy for translations was between ± 0.008 mm and ± 0.034 mm, while rotational accuracy was ± 0.082 deg to ± 0.160 deg. These results demonstrate that simultaneous optical measurement of 3D soft tissue strain and 3D joint kinematics can be performed while achieving excellent accuracy for both sets of measurements.

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Introduction

The measurement of strain is of fundamental interest in the study of soft tissue mechanics. In studies of musculoskeletal joint

mechanics, the accurate measurement of three-dimensional joint kinematics is equally important. By simultaneously quantifying the strains in soft tissues such as ligaments and the joint kinematics in response to externally applied loads, it is possible to elucidate the role of these structures in guiding and restraining joint motion and to identify potential injury methods and clinical treatments [1–3]. Further, simultaneous acquisition of joint kinematics and strain fields can be used to drive and validate subject-specific models of ligament and joint mechanics [4].

The simultaneous measurement of joint kinematics and soft tissue strain is typically accomplished by using a combination of two or more different technologies. Joint kinematics are commonly quantified using video-based techniques [5,6], instrumented spatial linkages (ISLs) [7,8], or electromagnetic tracking systems [9–11]. ISL systems require the attachment of a bulky mechanical linkage across the joint, while electromagnetic tracking systems are often plagued by interference from ferrous materials, limiting their applicability. In contrast, there are relatively few techniques that are capable of measurement of three-dimensional soft tissue strains. Alternatives include the use of one-dimensional measurements from contact devices such as DVRTs [12,13]. Optical methods are currently considered to be the best option for 3D strain measurement on visible soft tissues. These methods use the direct linear transformation to calculate 3D strain measurements from two or more cameras [4,14]. Previous optical systems were primarily based on super-VHS video, yielding an effective vertical resolution of 400 lines. This limited resolution requires the use of extremely small fields of view to achieve accuracies of ± 0.1 – 0.5% error in percent strain [14]. This precludes the simultaneous tracking of markers for kinematic measurements, since a larger field of view is needed to see both the strain and kinematic markers. Currently available systems based on digital cameras typically use vendor-supplied proprietary cameras and/or framegrabbers. These systems primarily use digital cameras that have much better resolution and sensitivity than video-based systems. However, the use of proprietary vendor-supplied hardware is often costly and ties the support and upgrade of the system to a particular vendor or system integrator.

Due to ongoing improvements in the sensitivity and resolution of charge-coupled devices (CCDs), modern progressive-scan digital cameras can provide images with very high quality and resolution. The improved spatial resolution (typically at least 1024×1024) opens up the possibility of using a field of view that is large enough to track markers for both soft tissue strain and joint kinematics. The use of cameras and framegrabbers from individual vendors is especially attractive since it eliminates the need for proprietary, vendor-specific hardware and software. The objective of this study was to develop a methodology for simultaneous measurement of three-dimensional (3D) soft tissue strain and joint kinematics using a nonproprietary digital camera system, and to quantify the errors associated with these measurements in a test setup that mimicked the study of knee ligament biomechanics.

Materials and Methods

Measurement System. The measurement system consisted of two high-resolution digital cameras [Pulnix TM-1040, $1024 \times 1024 \times 30$ frames per second (fps), Sunnyvale, CA] equipped with 50 mm 1:1.8 lenses and extension tubes, two framegrabbers (Bitflow, Woburn, MA) and Digital Motion Analysis Software (DMAS, Spica Technology Corporation, Maui, HI). The cameras were configured to record 6 fps directly to computer memory, requiring 2.1 MB of memory per frame. The cameras were focused at a target with a 190 mm diagonal field of view (FOV). The DMAS software tracked marker centroids in both camera views automatically and applied the modified direct linear transformation (DLT) to calculate the 3D centroid coordinates [15]. Preliminary tests demonstrated that black markers against a white background provided superior contrast and therefore system accuracy in comparison to markers covered with reflective tape, while

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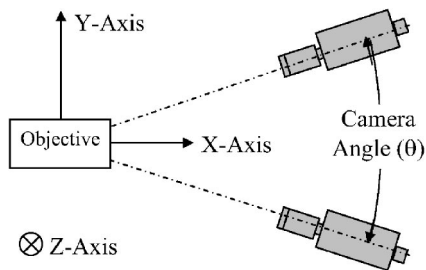


Fig. 1 Plan view of the camera setup. The z axis is directed out of the page. To assess system sensitivity to camera angle, angles of 30, 60, and 90 deg were used during testing.

two 100 W incandescent lights provided better contrast than halogen or fluorescent lighting. In the following sections, all instrument accuracy values are per the manufacturer.

A 3D calibration frame was manufactured. Twenty-seven white Delrin spherical markers (4.75 mm diameter) were arranged in three horizontal planes, with a 3×3 grid pattern on each plane and 60 mm marker spacing. The exact coordinates of each marker centroid were determined with a coordinate measuring machine (Zeiss Eclipse 4040, accuracy ± 0.0004 mm). These coordinates were used for DLT calibration.

Precision. The precision was determined by examining the variation of the 3D positions of stationary markers over time. After calibration, two different frames with twelve 4.75 and 2.38 mm diameter spherical markers were recorded for 25 s. The dimensions of these markers were chosen to be the exact same size as the kinematic markers (4.75 mm diam) and the strain markers (2.38 mm diam) used during actual biomechanical testing in our laboratory. The variation in marker position was determined by computing two standard deviations of the length of their position vector and the individual x , y , and z coordinates over time. Experiments were repeated at camera angles of 30, 60, and 90 deg (Fig. 1). To evaluate the precision of the system in actual test conditions, the variation of kinematic (4.75 mm diameter) and strain (2.38 mm diameter) marker positions were determined for four sets of 3-s passive recordings taken at a 30 deg camera angle

during biomechanical testing of a human medial collateral ligament (MCL) (Fig. 2). Complete details of this test configuration and marker placement can be found in our previous publications [4,14].

Accuracy of Simulated Strain Measurement. Accuracy tests were performed dynamically to determine the ability of the system to measure simulated 3D changes in strain. The effects of strain magnitude and camera angle were assessed. A 2.38 mm diameter marker was adhered to a fixed location, while a similar marker was adhered 13.5 mm apart (L_{initial}) to a linear actuator (Tol-O-Matic, Inc, Hamel, MN, accuracy ± 0.0025 mm). The L_{initial} was chosen to replicate the spacing between markers used to calculate 3D strains in the human MCL [4,14]. In two separate tests, the actuator was translated (ΔL) along either the z - or x axis in Fig. 1 to simulate strains of 1%, 2%, 5%, and 20%. Tests were performed four times for each displacement. Accuracy was calculated as the difference between the predicted displacement and the known actuator displacement. The error in simulated strain measurement was computed by determining the absolute difference between actuator strain and DMAS strain ($\Delta L/L_{\text{initial}}$).

Accuracy of Kinematic Measurements. When tracking joint kinematics, it is desirable to establish “embedded” coordinate systems within the bones using a convention such as the one described by Grood and Suntay [16]. The transformation matrix between embedded coordinate systems is established by tracking markers on the bones that define separate “marker” coordinate systems. The transformation between one marker coordinate system and the corresponding embedded coordinate system on a bone does not change during testing. By establishing these transformations before testing and then tracking the transformation between marker coordinate systems during testing, the transformation between embedded coordinate systems can be determined [4,14]. To assess kinematic measurement accuracy, the setup and calculations necessary to record knee joint kinematics were simulated. Two L-shaped white blocks (the “kinematic blocks,” Fig. 2) with three 4.75 mm diameter black markers that formed a 90 deg angle were used to establish marker coordinate systems. The following tests were repeated four times for each translation or rotation, at camera angles of 30, 60, and 90 deg.

To measure accuracy of translations along the z axis in Fig. 1

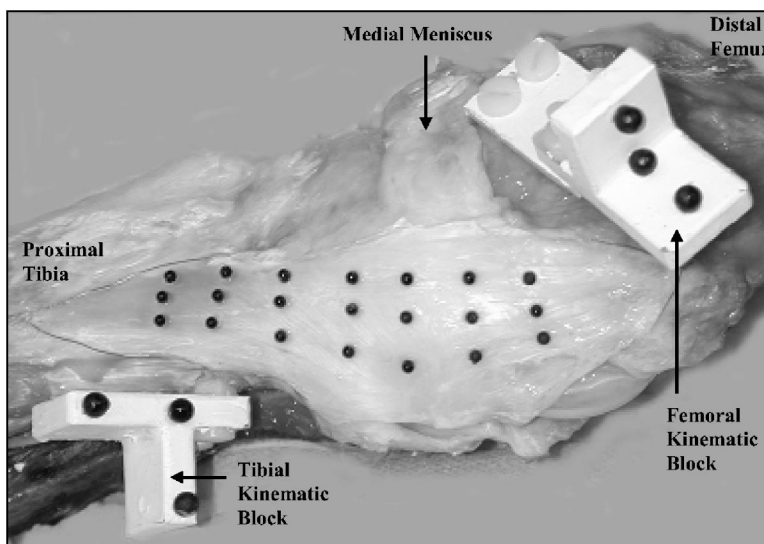


Fig. 2 Photograph of test setup for simultaneous measurement of MCL strain and knee joint kinematics. Eighteen markers (2.38 mm diameter) were adhered to the MCL for strain measurement. Femoral and tibial kinematic blocks, each with three kinematic markers (4.75 mm diameter), were affixed to the cortical bone.

Table 1 Results for measurement of 3D precision. The first three rows of data were obtained by recording stationary markers for 25 seconds with a FOV of 190 mm. The fourth row was obtained from passive recording acquired during biomechanical testing of a human MCL. Each passive recording was approximately 3 s long, with a camera angle of 30 deg, and a FOV of 190 mm. Absolute precision was calculated as two standard deviations of the position measurement, while percent FOV was calculated as the precision divided by the FOV multiplied by 100.

Camera angle (θ)	4.75 mm diam. markers		2.38 mm diam. markers	
	Precision (mm)	Percent FOV (%)	Precision (mm)	Percent FOV (%)
30 deg	0.004	0.0020%	0.035	0.0163%
60 deg	0.011	0.0049%	0.025	0.0117%
90 deg	0.006	0.0026%	0.012	0.0048%
MCL	.009	0.0044%	0.011	0.0054%
Study (30 deg)				

from kinematic calculations, one kinematic block was adhered to a static fixture and a second one was attached to the linear actuator. An Inscribe 3D Digitizer (Immersion Corp, San Jose, CA accuracy ± 0.085 mm) was used to determine the centroids of the markers by digitizing points on the marker surface and then fitting the coordinates to the equation of a sphere. To simulate the use of embedded coordinate systems, three points on both the static fixture and the actuator were digitized and used to establish ortho-normal coordinate systems. The transformation matrices were calculated between the kinematic blocks and their respective embedded coordinate systems. The actuator was displaced 0.500, 1.000, 5.000, and 50.000 mm and an overall transformation matrix between the embedded systems was calculated by concatenation. The ratio of the calculated translations to the known translations was computed.

To measure accuracy of translation measurements along the x axis in Fig. 1 from kinematic calculations, a kinematic block was adhered to an $x-y$ table and the table was moved 0.50, 1.00, 5.00, and 50.00 mm, measured with digital calipers (Mitutoyo, San Jose, accuracy ± 0.02 mm). Error was calculated as the ratio of translation predicted from the motion analysis data to the known translation.

To determine accuracy of rotations about the z axis in Fig. 1, a rotational actuator (Tol-O-Matic, Inc, Hamel, MN, accuracy ± 0.002 deg) was used to rotate one of the kinematic blocks through angles of 2.00 deg and 20.00 deg. The transformation matrix between the two embedded coordinate systems was calculated and the rotation between the two systems was resolved using

the method of Grood and Suntay [16]. The ratio of the rotation angle from the motion analysis data to the known angle was determined.

Statistical Analysis. The effects of camera angle and marker size on 3D precision were assessed using a two-way ANOVA with repeated measures. The effects of camera angle and strain magnitudes on x -axis and z -axis strain accuracy were assessed using two separate two-way ANOVAs with repeated measures. The effects of camera angle on x -axis and z -axis translational kinematic accuracy and z -axis rotational kinematic accuracy were assessed using two separate two-way ANOVAs with repeated measures. Statistical significance was set at $p < 0.05$ for all analyses.

Results

Precision. Results for precision were excellent for both marker sizes (Table 1). The larger markers exhibited significantly better precision than the smaller markers ($p = 0.005$). There was no effect of camera angle on marker precision ($p = 0.089$). The best results (± 0.004 mm, 0.0020% FOV) were obtained for the larger markers using a 30 deg camera angle. Precision did not vary considerably between the x , y , and z coordinates of the markers. For example, at a 60 deg camera angle, the larger markers had x , y , and z coordinate precisions of 0.019, 0.019, and 0.012 mm, respectively. The precisions for both marker sizes obtained with an MCL biomechanical test setup were comparable to precisions for the controlled tests (Table 1, fourth row of data).

Accuracy of Simulated Strain Measurement. The optical system delivered excellent results for strain error (Table 2). There was a significant effect of camera angle on accuracy for z - and x -axis strain accuracy ($p = 0.004$ and $p < 0.001$, respectively, Fig. 3). The most accurate camera angle for strains along the z axis was 30 deg, having an average accuracy of ± 0.005 mm with a strain error of $\pm 0.035\%$. Conversely, the most accurate camera angle when strains were measured along the x axis was 90 deg, having average accuracies of $\pm 0.003\%$ resulting in a strain error of $\pm 0.025\%$. There was a significant effect of strain magnitude on accuracy for z - and x -axis strain accuracy ($p = 0.008$ and $p < 0.001$, respectively). The condition conferring the least accuracy occurred for both the z -axis and x -axis cases at 90 deg and 30 deg, respectively, when a 20% strain was applied.

Accuracy of Kinematic Measurements. The optical system delivered very good results for kinematic accuracy (Table 3). Data for z -axis kinematic accuracy are shown as an example (Fig. 4). The average x - and z -axis translational accuracies across all three camera angles and all four actuator displacements were ± 0.025 mm and ± 0.016 mm, respectively. Average accuracy for rotation was ± 0.124 deg (Table 3). There was a significant effect of cam-

Table 2 Accuracy of 3D simulated strain measurement along the z - and x axes for all four strain levels. Accuracy (mm) was calculated as the difference between the actuator-based value and the value calculated from the optical system data. Strain error (%) is the accuracy divided by the gauge length (13.5 mm) multiplied by 100.

Camera angle (θ)			1.0% Strain	2.0% Strain	5.0% Strain	20.0% Strain	Averages across all Strains
z axis	30 deg	Accuracy (mm)	0.004 \pm 0.007	0.011 \pm 0.003	0.003 \pm 0.004	0.001 \pm 0.007	0.005\pm0.005
		Strain error (%)	0.028 \pm 0.052	0.084 \pm 0.018	0.019 \pm 0.030	0.010 \pm 0.052	0.035 \pm 0.033
	60 deg	Accuracy (mm)	0.002 \pm 0.001	0.013 \pm 0.005	0.005 \pm 0.005	0.009 \pm 0.012	0.007\pm0.006
		Strain error (%)	0.014 \pm 0.009	0.099 \pm 0.037	0.040 \pm 0.035	0.067 \pm 0.091	0.055 \pm 0.037
	90 deg	Accuracy (mm)	0.009 \pm 0.001	0.016 \pm 0.003	0.011 \pm 0.004	0.024 \pm 0.005	0.015\pm0.003
		Strain error (%)	0.065 \pm 0.006	0.115 \pm 0.025	0.081 \pm 0.027	0.175 \pm 0.034	0.109 \pm 0.049
x axis	30 deg	Accuracy (mm)	0.011 \pm 0.002	0.011 \pm 0.002	0.019 \pm 0.002	0.036 \pm 0.003	0.019\pm0.012
		Strain error (%)	0.081 \pm 0.018	0.082 \pm 0.014	0.138 \pm 0.017	0.267 \pm 0.024	0.142 \pm 0.088
	60 deg	Accuracy (mm)	0.002 \pm 0.002	0.018 \pm 0.002	0.006 \pm 0.011	0.003 \pm 0.002	0.007\pm0.007
		Strain error (%)	0.015 \pm 0.015	0.130 \pm 0.017	0.045 \pm 0.082	0.021 \pm 0.011	0.053 \pm 0.053
	90 deg	Accuracy (mm)	0.002 \pm 0.001	0.006 \pm 0.001	0.003 \pm 0.007	0.003 \pm 0.001	0.003\pm0.002
		Strain error (%)	0.017 \pm 0.008	0.045 \pm 0.007	0.022 \pm 0.049	0.018 \pm 0.006	0.025 \pm 0.013

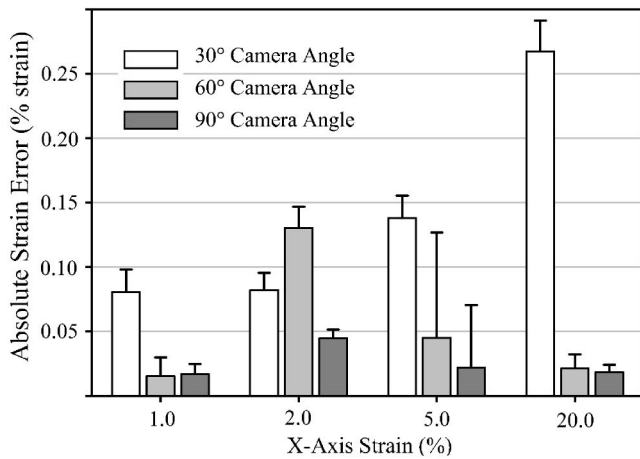
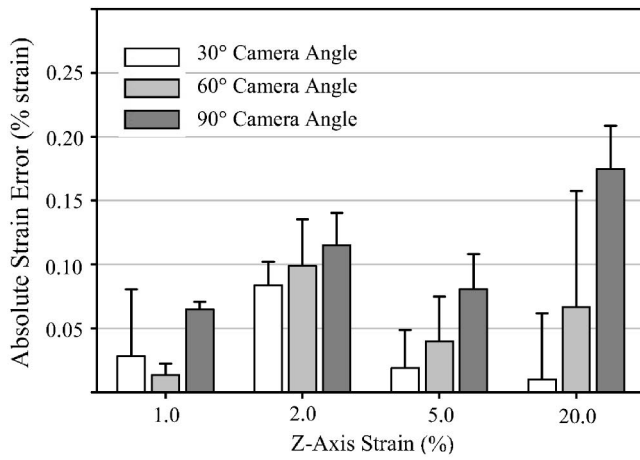


Fig. 3 Results for determination of simulated 3D strain along the z- and x axes. Strain error was computed as the difference between the actuator-based strain and the strain calculated by the motion analysis system, divided by the gauge length.

era angle on accuracy of kinematic measurements of translation along the z- and x axes ($p = 0.029$ and $p < 0.001$, respectively), but there was no effect of camera angle on kinematic rotational accuracy ($p = 0.378$). The effect of camera angle on the kinematic translational accuracies was similar to that for the strain accuracies. There was a significant effect of the magnitude of translation/rotation on accuracy of kinematic measurements of translation along the z- and x axes and rotation about the z axis ($p < 0.001$, $p < 0.001$, and $p = 0.033$, respectively). Larger translations/rotations reduced kinematic accuracy.

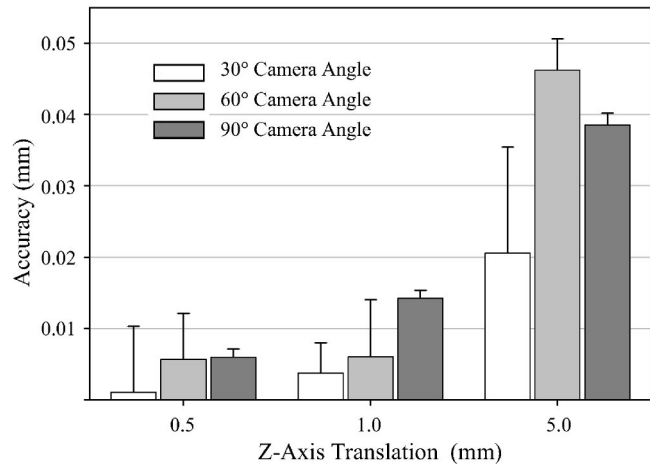


Fig. 4 Results for the measurement of 3D kinematics along the z-axis direction. Accuracy was measured as the difference between the actuator-based translation and the value calculated by the motion analysis system, divided by the actuator translation.

Discussion

This study demonstrated that the 3D system can accurately measure simulated strain and kinematics using physical and optical conditions that accommodate simultaneous tracking of markers for both measurements. A reduced camera angle significantly improved accuracy for frontal plane (z axis) displacements, while an increased camera angle significantly improved accuracies of displacements along the intersection of the sagittal and transverse planes (x axis). Moreover, in comparison to similar systems using proprietary vendor-specific hardware, this system is a small fraction of the cost.

Accuracy and precision of the system were determined using a testing environment that was specifically designed to mimic the physical and optical conditions for experiments on the human MCL in intact knees. For actual testing of the human MCL, only precision was determined. It is not possible to determine strain accuracy during an actual biomechanical test since a gold standard for strain measurements is difficult if not impossible to establish. However, by setting all testing variables (i.e., FOV, marker size, marker spacing, lighting) appropriately, the controlled tests faithfully reproduced the physical and optical conditions of actual biomechanical tests for the MCL. Results for precision from the controlled tests and from actual measurements on the MCL were similar (Table 1), supporting the notion that the controlled tests provided a good surrogate for the physical and optical conditions that are encountered during actual tests on the MCL.

System precision (Table 1) was calculated using the length of the position vectors of the markers, and thus these measurements

Table 3 Accuracy of 3D kinematic measurements. Accuracy is the difference between the actuator translation/rotation and the value calculated from the optical system data. Accuracy in terms of percent FOV is the accuracy divided by FOV multiplied by 100. Results are the average across all translations/rotations described in the Methods section.

Camera angle (θ)	Translation (x axis)		Translation (z axis)		Rotation (z axis)	
	Accuracy (mm)	% FOV	Accuracy (mm)	% FOV	Accuracy (deg)	% FOV
30 deg	0.034±0.031	0.012±0.004%	0.008±0.011	0.005±0.006%	0.132±0.162	0.074±0.091%
60 deg	0.018±0.005	0.009±0.006%	0.019±0.023	0.009±0.010%	0.082±0.069	0.043±0.036%
90 deg	0.021±0.002	0.009±0.008%	0.020±0.017	0.006±0.005%	0.160±0.218	0.074±0.101%

should be considered average errors that take into account the precision in all three spatial directions. For the simulated strain measurements, the major spatial directions were accounted for by testing along the x - and z axes. By positioning the cameras at an angle that permitted the most marker motion perpendicular to the cameras, therefore reducing the incremental distances that each pixel in the video system represents, the strain error was significantly decreased. For z -axis strains this occurred at a 30 deg camera angle, and for x -axis strains this occurred at a 90 deg camera angle. Based upon the accuracy results (Fig. 3), it is recommended that these camera angles are optimized accordingly, especially if large strains are predicted. The measurements of strain accuracy should be considered a best case when considering general measurements in 3D using comparable camera angles. Although a similar argument applies to the kinematic measurements, the "gold standard" for these measurements was based on a combination of digitizer, actuator encoder, or digital caliper measurements. Because of differences in the accuracy of these measurement techniques and the propagation of errors in the kinematic measurements, the results for translational and rotational kinematic accuracies likely represent worst cases. This error propagation is likely responsible for the reduction of accuracy with increased axial translation (Fig. 4).

As with any system based on video or digital cameras, the most important determinants of precision and accuracy are the resolution of the CCD and the FOV used for measurements. This assumes that an accurate DLT calibration has been performed and that this calibration has taken into account errors associated with lens distortion. In this study, the FOV was chosen to allow simultaneous tracking of markers for strain and kinematic measurements in the context of studying the human MCL [4,14]. Limitations on the rate of data transfer from the camera to the framegrabber cards and then to computer memory, primarily imposed by the bandwidth of the computer system's bus, result in a trade-off between the frame rate and spatial resolution of the CCD. Cameras with higher resolution CCDs typically have slower frame rates. This limitation will likely be eliminated with improvements in computer architecture. Marker contrast is also very important, with improved contrast yielding better system precision and thus accuracy. During actual biomechanical testing, contrast may become reduced by extraneous objects in the foreground and background. Draping the testing backdrop and fixtures with white material, and applying white gauze to any uninvolved tissue that may darken the captured image will alleviate this problem. Extreme specimen discoloration could similarly reduce marker contrast. Affixing the strain markers to the tissue with adhesives may cause local strain abnormalities; therefore, a minimal amount of adhesive should be applied. Finally, the physical size of a CCD affects the sensitivity through its responsivity and dynamic range, with larger CCDs yielding better sensitivity and thus better image quality (see, e.g., [17]). The cameras used in this study had 1 in. CCDs, the largest size that was available.

In summary, the 3D measurement system provided excellent accuracy for simulated strain measurement and very good accu-

racy for kinematic measurements. The absolute and percent errors are considered to be more than acceptable for simultaneous 3D measurements of ligament strain and joint kinematics.

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